Digital signal processing approaches for semiconductor phase noise tolerant coherent transmission systems

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ABSTRACT

We discuss about digital signal processing approaches that can enable coherent links based on semiconductor lasers. A state-of-the-art analysis on different carrier-phase recovery (CPR) techniques is presented. We show that these techniques are based on the assumption of lorentzian linewidth, which does not hold for monolithically integrated semiconductor lasers. We investigate the impact of such lineshape on both 3 and 20 dB linewidth and experimentally conduct a systematic study for 56-GBaud DP-QPSK and 28-GBaud DP-16QAM systems using a decision directed phase look loop algorithm. We show how carrier induced frequency noise has no impact on linewidth but a significant impact on system performance; which rises the question on whether 3-dB linewidth should be used as performance estimator for semiconductor lasers.

Keywords: optical communications, coherent communications, phase noise

1. INTRODUCTION

Cloud services have already revolutionized the way modern societies interact, yet this is just the beginning of a much bigger data communication revolution. Smart-grid, smart-city and autonomous transportation are feasible near-term solutions to reduce global energy consumption and therefore our environmental footprint. These approaches rely on enormous amounts of data being sensed and transported throughout the city, alongside next generation broadband services, compromising the ability of current metropolitan area networks to cope up with bandwidth demands. Pushing coherent technologies towards the end-user could effectively tackle the problem, but the strong requirements on laser linewidth make them rely on costly external cavity lasers (ECLs), rendering the transceiver economically nonviable for metro-access scenarios. Monolithically integrated semiconductor lasers on the other hand, are generally more cost-effective, energy efficient, and easy to integrate, at the expense of higher linewidths due to carrier induced frequency noise. Consequently, realizing cost-competitive coherent data-links on the range of 100-500 km based on semiconductor lasers has become a timely research question.

Digital signal processing (DSP) is one of the key technologies that enabled the commercialization of coherent technologies on the past decade.\(^{1}\) A critical block in the DSP chain is the CPR. It is normally the last block before symbol decision takes place, and it is in charge of compensating for the laser phase noise, which is directly related to the frequency noise. Typically, those algorithms are evaluated in terms of optical signal-to-noise ratio (OSNR) penalty versus the laser linewidth times the symbol period of the transmitted signal \((\Delta_\nu \tau)\). The laser linewidth is the full width half maximum (FWHM) of its optical spectrum. It is an important figure of merit for lasers generally used to quantify the amount of frequency noise that is present in a coherent transmission link, which plays an important role on system performance.\(^{2}\) Under the assumption of spectrally flat white frequency noise, the laser linewidth is directly proportional to the power of the frequency noise.\(^{3}\) This assumption holds relatively well for ECLs, which are often used in coherent transceivers as they can provide very narrow linewidths.\(^{4}\) For that reason, it makes sense to use \((\Delta_\nu \tau)\) to benchmark CPR algorithms. On the other hand, when considering monolithically integrated semiconductor lasers, the power spectral density of the frequency noise is no longer

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flat, and hence the relationship between linewidth and frequency noise is no longer trivial.\cite{5,6} Hence, it is an open question whether linewidth is a good estimator of performance in this case.

In this paper, we review the state of the art in CPR techniques and investigate the relation between frequency noise power spectral density, laser linewidth, and system performance when semiconductor lasers are considered. We first derive a frequency noise model that takes into account carrier induced frequency noise and flicker noise. Then, we numerically calculate the laser lineshape while varying different parameters of the model, and analyze the impact on 3-dB and 20-dB linewidths. Finally, we experimentally investigate the impact of different frequency noise profiles on system performance for 28 and 56 Gbaud QPSK systems.

2. CARRIER PHASE RECOVERY TECHNIQUES

The most optimum phase estimator that we can use is the maximum a posteriori (MAP).\cite{7} This involves estimating both the data (symbols) and the phase, and it is not feasible for real-time DSP implementation in a coherent receiver. Nevertheless this method provides an optimum performance as a reference for other methods. Practical implementations of CPR algorithms estimate the phase separately from the data. That means that the data must be removed from the phase noise sequence before the estimation process begins. This can be achieved by using either feedback or feedforward loops. A commonly used algorithm that belongs to the feedback family is the decision directed phase lock loop (DDPLL),\cite{8,11} where the phase estimator uses the estimated carrier phase of a previous symbol to derotate the current symbol, feeding the result into a decision block. This method has the advantage of being able to track the phase, allowing for moderate frequency offset compensation and reducing the probability of cycle slips. However, for this to be effective, the feedback delay needs to be very low, which imposes several challenges for real time implementation. Decision aided maximum likelihood (DA ML)\cite{12,13} is another feedback based algorithm that is more tolerant to non-linear phase noise. Although computationally less demanding, its performance is still tightly related to the feedback delay. Recently, Kalman filtering has been proposed for CPR.\cite{14} It can be seen as a generalized DDPLL where the loop gain is variable and both the phase and the amplitude are estimated. This method was compared to feedforward structures and was shown to outperform them at low OSNR values. A more practical approach to CPR for implementation purposes is the feedforward structure, since it avoids the need for feedback delays.\cite{15} The most popular technique is the so-called Viterbi & Viterbi algorithm,\cite{16} which works best for M-phase-shift keying (PSK) signals. The algorithm removes the data information by squaring the received sequence to the $M^{th}$ power, and estimates the phase by calculating the average phase of the resulting cluster in the constellation and dividing it by $M$. The simplicity of this method is overshadowed by its computational complexity due to the non-linear operations, and its inapplicability to quadrature amplitude modulation (QAM) signals. This last disadvantage was quickly overcome with the two-stage quadrature phase-shift keying (QPSK) partitioning scheme.\cite{17} The use of two-stage feedforward techniques is now gaining popularity. The first stage is aimed to erase the modulation data whereas the second stage is used to estimate the phase.\cite{18,19,20} Blind phase search (BPS) is a simple method used in the second stage. It is a brute force approach in which a finite number of test phases are applied to the constellation until minimum error vector magnitude (EVM) is reached.

All of these techniques, however, assume lorentzian linewidth; and their performance may be degraded in presence of high carrier induced frequency noise. It is therefore necessary to study the influence of semiconductor frequency noise on both laser linewidth and system performance.

3. SEMICONDUCTOR LASER FREQUENCY NOISE MODEL

The short-term phase variation of a waveform, can be represented either as phase or frequency noise. Frequency noise refers to random fluctuations of the instantaneous frequency, which is the temporal derivative of the phase. We model the single-sided power spectral density of frequency noise as:

$$S_\nu(f) = \frac{10^9 \Delta_\nu(1/f)}{\pi f} + \frac{\Delta_\nu_{int}}{\pi(1 + \alpha^2)} \left(1 + \alpha^2 \frac{f_R^4}{(f_R^2 - f^2)^2 + \left(\frac{K f_R^2}{2\pi f}\right)^2}\right) \quad (1)$$

where:
Figure 1: (left) Frequency noise power spectral density (PSD) for $\Delta_{v(1/f)} = 10$ kHz, $\Delta_{vint} = 100$ kHz, $f_R = 10$ GHz, $K = 0.15$ ns and $\alpha = 3$. (right) Phase noise PSD obtained by dividing $S_{\nu}(f)/f^2$

- $\Delta_{v(1/f)}$ describes the level of $1/f$ noise at 1 GHz.
- $\Delta_{vint}$ describes the level of the intrinsic frequency noise at low frequencies.
- $f_R$ is the resonance frequency.
- $K$-factor describes how the damping rate increases with relaxation frequency. The $K$-factor of semiconductor lasers is approximately bias independent and in the range of 0.1-1 ns.
- $\alpha$ parameter determines the level of white frequency noise beyond the resonance frequency.

Figure 1 shows the frequency and phase power spectral density (PSD) for a frequency modulation (FM) noise model with parameters $\Delta_{v(1/f)} = 10$ kHz, $\Delta_{vint} = 100$ kHz, $f_R = 10$ GHz, $K = 0.15$ ns and $\alpha = 3$. It is a common practice to scale the result by $\pi$ in order to match the intrinsic linewidth ($\Delta_{vint}$) with what would be the 3-dB linewidth if the lineshape was Lorentzian. The phase noise PSD is obtained by simply dividing the frequency noise PSD by $f^2$.

4. IMPACT ON LINEWIDTH

If the frequency noise PSD is known, the optical spectrum can be calculated as the Fourier transform of the autocorrelation function:

$$S_{\nu}(\Delta \nu) = \text{Fourier}[R(\tau)] \propto \text{Fourier} \left\{ \exp \left[ -2(\pi \tau)^2 \int_0^{\infty} S_{\nu}(f) \left| \frac{\sin(\pi f \tau)}{\pi f \tau} \right|^2 df \right] \right\}$$  \hspace{1cm} (2)

where $S_{\nu}(\Delta \nu)$ is the optical spectral density, $\Delta \nu = \nu - \nu_0$ is the optical frequency measured with laser frequency $\nu_0$ as a reference, and $S_{\nu}(f)$ is the frequency noise PSD as described in section 3.

Figure 2 shows the calculated optical lineshape for different frequency noise PSDs. For the blue curve, only spectrally flat white frequency noise is considered. This yields to a Lorentzian lineshape with a 3-dB linewidth of $\pi h_0$, where $h_0$ is set to 100 kHz. The red curve also includes $1/f$, or flicker noise. In this case, Eq 2 cannot be analytically solved and the linewidth must be numerically calculated. Lastly, the green-dashed curve includes the carrier induced frequency noise as well. It is noteworthy how the last effect has no influence on either 3 or 20 dB linewidth. To further investigate this, we performed several sweeps and observed the impact of lorentzian on the 3 and 20 dB linewidth. Table 1 shows the parameters of the model as well as the ranges of each sweep.
Each parameter is swept while keeping the rest of the parameters fixed to their default value. The results are presented in figure 3. We can observe a linear relation with respect the $S_\nu(\Delta \nu)$ (figure 3a). This is due to the fact that this parameter scales the amount of white frequency noise evenly throughout the FM noise spectrum.

In case of $\Delta \nu_{1/f}$ (figure 3b), the 3 and 20 dB linewidths take the shape of $\sqrt{\Delta \nu_{1/f}}$. For $f_R$ parameter, we observe a 0.15 dB deviation at low resonance frequencies for the 20 dB linewidth, and no deviation above 2 GHz.

As for $K$ and $\alpha$ parameters (figures 3d and e), there is no impact on either 3 or 20 dB linewidth for the values under study.

### Table 1: Parameters for linewidth sweeps

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Default</th>
<th>Range</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta \nu_{1/f}$</td>
<td>100</td>
<td>100 - 900 kHz</td>
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</tr>
<tr>
<td>$\Delta \nu_{int}$</td>
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<td>1 - $10^4$ Hz</td>
<td></td>
</tr>
<tr>
<td>$f_R$</td>
<td>10</td>
<td>1 - 10 GHz</td>
<td></td>
</tr>
<tr>
<td>$K$</td>
<td>0.15</td>
<td>0.1 - 1 ns</td>
<td></td>
</tr>
<tr>
<td>$\alpha$</td>
<td>3</td>
<td>0.1 - 10 -</td>
<td></td>
</tr>
</tbody>
</table>

5. IMPACT ON SYSTEM PERFORMANCE

The effect of each parameter should be study in terms of system performance. Intrinsic linewidth is studied in most of the studies reviewed in section 2. The relation depends on the specific CPR technique but tends to be linear.\textsuperscript{7} $1/f$, or flicker noise has also been extensively studied,\textsuperscript{22-24} where the penalty seems to increase exponentially with the amount of $1/f$ noise. For carrier induced frequency noise, however, no studies has been

![Figure 3](http://spiedigitallibrary.org/)
found on system performance. This noise is mainly governed by the resonance frequency and the K-factor and is the main topic of our research. In our previous experiments, the impact of semiconductor laser frequency noise was systematically studied on 28 and 56 Gbaud DP-QPSK systems with up to 500 km standard single mode fiber (SSMF). The experimental setup is detailed in Ref. 21 and consisted of a standard DP-QPSK transmitter and receiver, with 100 kHz external cavity lasers used for both the local oscillator and the transmitter. To emulate specific phase noise profiles, we used a LiNbO3 phase modulator and an arbitrary waveform generator at 50 GS/s to control the phase noise spectrum of the transmitter laser. For data demodulation, we use the a standard DSP chain based on. The CPR algorithm used was a standard DDPLL based on. 25

Figure 4 summarizes the results in back to back (B2B) configuration. The 3D plots show the penalty with respect to OSNR at the receiver sensitivity under no added phase noise, for different phase noise conditions, where the x-axis represents $f_R$ for 1, 3 and 5 GHz. The y-axis represents the $K$-factor for 0.1, 0.5 and 1 ns. And the z-axis represents $\Delta v_{int}$ for 0.5, 5 and 10 MHz. The OSNR penalty is color coded, where a larger intensity represents larger penalty. We define the receiver sensitivity at a BER of $2 \cdot 10^{-3}$. The OSNR values at this baudrate under no added phase noise were 11.3 and 14.5 dB for 28 and 56 Gbaud respectively; both B2B and after 500 km SSMF. A total of 27 BER curves were measured from where the OSNR at receiver sensitivity was obtained. This was measured for both 28 Gbaud (left) and 56 Gbaud (right) DP-QPSK, both B2B and after 500 km SSMF with no observable penalty due to transmission. Three cases were selected covering all values for the parameters [$f_R, K, \Delta v_{int}$], under study, from the worst case to the best. The cases are defined as $a = [1, 0.1, 10]$, $b = [3, 0.5, 5]$ and $c = [5, 1, 0.5]$ for both 28 and 56 Gbaud signals. The frequency noise power spectral density $S_v(f)$ of each case is also presented in Fig 4. The position of the labels within the plot also indicates the position of each resonance frequency. A reference spectrum without any added phase noise is also included. In addition, the received constellations for the x-polarization at each case are presented. Note that, for the 28 Gbaud DP-QPSK signal, the obtained BER in case a) was below the sensitivity, and therefore the OSNR is represented as not a number (NaN). On the other hand, the penalty observed between the reference phase noise and case c) was negligible.

The results show that the influence of the resonance peak has a major impact on system performance. As expected, the penalty is reduced as the baudrate is increased. It is interesting to observe that up to 10 MHz of intrinsic linewidth can be tolerated within 0.5 dB penalty as long as the resonance frequency and the K-factor are above 3 GHz and 0.5 ns respectively.
6. CONCLUSIONS
This paper addresses the status of CPR algorithms for semiconductor phase noise tolerant coherent transmission systems. A state-of-the-art review for CPR techniques is performed, concluding that most of the techniques are benchmarked against laser linewidth, which inherently assumes lorentzian lineshape. We then show how carrier induced frequency noise does not contribute to the 3 dB laser linewidth. However, it is identified that this type of noise plays an important factor on system performance. The results lead to the conclusion that 3 dB linewidth is not a good estimator of system performance for semiconductor laser frequency noise. Future lines of work include exploring the impact on 16-DPQAM systems and including the dynamics of carrier induced frequency noise on CPR algorithms. We identify Kalman CPR as one of the potential candidates to include this effect, although a feedforward structure would be preferred to reduce the DSP complexity.

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